Statistics on Structures 3

- Robustness evaluation in CAE with software optiSLang and Statistics on Structures
- Application examples
- New features
Robustness: Definition of uncertainties

- Translate knowledge about uncertainties into proper definition of randomness

Distribution functions define variable scatter

Correlation is an important characteristic of stochastic variables

Spatial Correlation = random fields
Typical quantities being random fields

- Examples
  - geometric perturbations
    - node coordinates
    - shell thickness
    - thickness of composite layers
  - material properties
    - concrete: mortar, admixtures (gravel)
  - damage
    - plastic strain
    - cracks
  - loading
  - state variables
    - stresses
    - strains
    - displacements
Robustness: Exceedance probability

Probability of reaching values above a limit

Gaussian distribution:

\[ P_\xi = P[X \geq \xi] \]

<table>
<thead>
<tr>
<th>( \xi )</th>
<th>( \mu )</th>
<th>( \mu + \sigma )</th>
<th>( \mu + 2\sigma )</th>
<th>( \mu + 3\sigma )</th>
<th>( \mu + 4\sigma )</th>
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<tr>
<td>( P_\xi )</td>
<td>( 5 \cdot 10^{-1} )</td>
<td>( 1.6 \cdot 10^{-1} )</td>
<td>( 2.3 \cdot 10^{-2} )</td>
<td>( 1.4 \cdot 10^{-3} )</td>
<td>( 3.2 \cdot 10^{-5} )</td>
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</table>
Variance based robustness analysis

1) Define the robustness space using scatter range, distribution and correlation

2) Sampling: Scan the robustness space by producing and evaluating $n$ designs

3) Check the variation

4) Check the explainability of the model

5) Identify the most important scattering variables
Software tool: Statistics on Structures (SoS)

- post processor for statistical analysis of data distributed on FEM meshes
- import/export meshes and data to LS-Dyna, NASTRAN, photos et al
- integration with optiSLang
- computes statistical quantities (mean, stddev, min, max, range, eroded data/cracks, quantile, etc.)
- determination of “hot spots”
- identification of spatial correlations through random fields, noise elimination, improved determination of input-output relations
- main area of applications: metal forming, car crash, brake pads
Statistics on Structures: Objectives

- Analyze random properties of structures
- Identify consequences of manufacturing tolerances and random loads
- Inspect statistics directly on the structure
- Improve robustness and product quality
- Easily detect hot spots and potential failure locations
- Improve analysis of the cause of scatter
- Create random designs
- Eliminate random noise
- Detect geometric perturbations
Robustness evaluation at hot spots

- Identify “hot spots”, eg. locations with large mean, large stddev or extremal quantile values
- Robustness evaluation at hot spots
- Sensitivity analysis at hot spots to find responsible input parameters
Robustness: Find input-output relations

- Sensitivity measured by analyzing scalar parameters in optiSLang
- Problems: FEM field quantities with >>1000 individual parameters, varying location of extrema
- Reduce number of parameters by Karhunen-Loeve expansion; Analyze sensitivity of Karhunen-Loeve coefficients; Visualize location of sensitivities through Karhunen-Loeve shapes
Simulation of random fields

- Simulation of random numbers at each FEM mesh point:
  - random geometric perturbations (node coordinates, shell thickness, layer thickness)
  - pre-damage/loading with random perturbations (plastic strain, pre-stress, etc.)

- Idea: 2 CAE processes: (1) Analyze random field (output), (2) Simulate random field (input)
Detection and export of geometric perturbations

- 2 CAE processes: Automation of using a random geometry (output of 1st) as input for the 2nd simulation
- Examples: 2 production steps or 1 production step + 1 load case, etc.
Statistics on Structures 3

Applications
Application: Crash simulation - cause analysis

- Stringer in a car body subject to crash simulation
- 55 random inputs: sheet thickness and material parameters (also of other parts), load parameters (velocity, barrier angle etc.)

max. plastic strain after crash

- Observed result: remaining effective plastic strain

Robustness analysis of structural crash load cases at Daimler AG
Application: Crash simulation - cause analysis

- Analysis of a car structure subject to random crash load case
- Decomposition of plastic strain random field
- Analysis of largest influence by MoP/CoP in optiSLang


Johannes Will (DYNARDO GmbH), Thomas Frank (Daimler AG), 2008

Robustness analysis of structural crash load cases at Daimler AG
Application: Drop test of a cell phone

- Tasks:
  - Find the most critical drop test position (angle) - sensitivity analysis
  - Robustness analysis with respect to material and production parameters

Alexander Ptchelintsev, Gerald Grewolls, Marcus Theman (NOKIA Corporation), Johannes Will (DYNARDO GmbH)
Applying sensitivity analysis and robustness evaluation in virtual prototyping on product level using optiSLang
SIMULIA Customer Conference, 2010
Application: RDO of a forming part (car body)

- sensitivity analysis, robustness evaluation and optimization
- LS-DYNA for forming simulation (50 min)
- parameters: 12 bead forces (0...350 N), tool binder force (50...300 kN)

Johannes Will (DYNARDO GmbH)
Robust Design Optimization in forming process simulation
Weimarer Optimierungs- und Stochastiktage 4.0, 2007
Application: Robustness evaluation in car crash

- Estimation of scatter of important result variables
- Identification of sensitive scattering input variables
- Quantification of influence of numerical noise on variation of result variables

displacements: C.o.D. and standard deviation

Johannes Will (DYNARDO GmbH), Uli Stelzmann (CADFEM GmbH)
Robustness Evaluation of Crashworthiness using LS-DYNA and optiSLang
25. CADFEM Users’ Meeting, 2007
Robustness of brake system to squeal noise

difference between measured and modeled geometry of a knuckle

Simulation of imperfect geometries

Identify a narrow range of values of the Young’s modulus of the pad being responsible for small damping

Ronaldo Nunes (Daimler AG), Johannes Will, Veit Bayer, Karthik Chittepu (DYNARDO GmbH)

Robustness evaluation of brake systems concerned to squeal noise problem
Weimarer Optimierungs- und Stochastiktage 6.0, 2009
Robustness of consecutive production processes

- multiple production steps:
  1. deep drawing
  2. several forming steps
- large failure rates during last forming step
- Simulation with FASTFORM
- observed quantity: thinning at critical location
- material parameter r90 as most sensitive input parameter

Johannes Will (DYNARDO GmbH), Tobias Menke, Andre Stühmeyer (CADFEM GmbH)
Rechnerische Robustheitsbewertungen von Umformprozessen
Internationale Konferenz "Neuere Entwicklungen in der Blechumformung", 2006

Johannes Will (DYNARDO GmbH), Prof. Christian Bucher (Bauhaus-Universität Weimar), Markus Ganser, Kathrin Grossenbacher (BMW AG), 2005
Computation and Visualization of Statistical Measures on FE Structures for Forming Simulations

S. Wolff: Statistics on Structures 3. WOST 2013
Application: Robustness evaluation of a car door

- car door - produced by metal forming
- original simulation: predict good robustness (Pf 1%), reality: different
- Identify better statistical description of parameters from 39 experiments
- simulation (sampling) and find hot spots
- compute Pf at hot spot 2: 25%
- Identify responsible input scatter:
  - MOP at hot spot with bad CoP
  - MOP based on Karhunen-Loeve expansion: high CoP

Hansjörg Lehmkuhl, Johannes Will, Vera Sturm, and Jörg Gerlach. Which discretization level for uncertainties do we need for reliable robustness evaluations in forming application? In 9th Weimar Optimization and Stochastic Days, Weimar, Germany, 2012. Dynardo GmbH.
Application: Identify geometry perturbations

- Given: deformed geometries of a metal forming simulation of a car cowling
- Detect deviations from the ideal reference geometry
- Karhunen-Loeve expansion of the deviations and create MOP for the respective scatter shapes
- Identify input parameters responsible for the perturbations

Will, J.
Integration of CAE-based optimization and robustness evaluation in virtual prototyping processes at Daimler using optiSLang,
Daimler EDM Forum, Stuttgart, 2013
Statistics on Structures 3

New features
New graphical user interface

- flexible
- SoS stores all imported designs and temporary results
- import additional designs after first analysis
- deactivate statistical outliers during analysis
Algorithms

- descriptive statistics (mean, stddev, cov, linear correlation, etc.)
- variable range (min, max, range)
- robustness measures (quantiles, QCS, exceedance probability, etc.)
- random fields, Karhunen-Loeve expansion (amplitudes, scatter shapes, noise elimination, generate random fields)
- eroded data (frequency of erosion)
- detection of geometric deviations between non-matching meshes
Visualization

- visualize up to 4 field objects at once
- highly configurable
- export renderings by various image formats or high resolution PDF
Technical features

- Operating systems: Windows 7 64 Bit, Linux 64 Bit (Redhat 6, SLES 11)
- Mesh coarsening: Not existing anymore
- Relaxed limitations on FEM mesh sizes (tested up to 500,000 elements)
- Improved numerical efficiency and memory consumption
- Full use of multi-core workstations by shared memory parallelization
- Portable binary format
- Embedded scripting (Lua)
- Batch processing on Linux servers (incl. graphics)
## File formats

<table>
<thead>
<tr>
<th>format</th>
<th>import</th>
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<tr>
<td>Native</td>
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<tr>
<td>binary data base, script</td>
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<td>scalar parameters</td>
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<td>yes</td>
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<td>optiSLang, CSV</td>
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<td>FEM mesh</td>
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<td>STL</td>
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<tr>
<td>FEM mesh + data</td>
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<tr>
<td>LS-Dyna, NASTRAN, PNG</td>
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<tr>
<td><em>AutoForm</em> through <em>LS-Dyna</em></td>
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Image processing

- Import photos (from measurements)
Summary

Statistics on Structures is the tool to answer the questions:

**Where?**
Locate hot spots of highest variation and/or extreme values, which may cause lack of performance or quality.

**Why?**
Find the input parameters which cause scatter of the results, by analyzing correlation/CoD between random inputs and spatially distributed results, export to optiSLang for MoP/CoP analysis, improve

Further it is the tool to

**Generate random designs**